

Electromagnetism - Coefficients of Reflection and Transmission at the interface between two non-magnetic non-conducting media

Reflection and Transmission coefficients are obtained using:

$$R = \frac{S_R}{S_I} = \frac{E_{OR}^2}{E_{OI}^2}$$

$$T = \left(\frac{\epsilon_{rel2}}{\epsilon_{rel1}} \right)^{1/2} \frac{E_{OT}^2 \cos \theta_T}{E_{OI}^2 \cos \theta_I} = \frac{n_2}{n_1} \frac{E_{OT}^2 \cos \theta_T}{E_{OI}^2 \cos \theta_I}$$

Using Fresnel's equations with $\mu_1 = \mu_2 = \mu_0$ this gives two sets of results depending on whether 1) \underline{E} is polarised normal to the plane of incidence or, 2) \underline{E} is polarised parallel to the plane of incidence:

$$1) \quad R_N = \left[\frac{\frac{n_1}{n_2} \cos \theta_I - \cos \theta_T}{\frac{n_1}{n_2} \cos \theta_I + \cos \theta_T} \right]^2$$

$$T_N = \frac{4 \frac{n_1}{n_2} \cos \theta_I \cos \theta_T}{\left[\frac{n_1}{n_2} \cos \theta_I + \cos \theta_T \right]^2}$$

$$2) \quad R_P = \left[\frac{-\cos \theta_I + \frac{n_1}{n_2} \cos \theta_T}{\cos \theta_I + \frac{n_1}{n_2} \cos \theta_T} \right]^2$$

$$T_P = \frac{4 \frac{n_1}{n_2} \cos \theta_I \cos \theta_T}{\left[\cos \theta_I + \frac{n_1}{n_2} \cos \theta_T \right]^2}$$

In both cases $R + T = 1$