# Dielectrics Examination questions 2005

## **SHORT QUESTIONS** [4 marks for each correct answer]

- a) What is the key structural requirement of a material in order to exhibit the piezoelectric effect? Give a simple illustration of a system which would show this effect.
- b) Sketch a plot of polarisation against electric field, labelling key points, for a ferroelectric material below and above the Curie temperature.

### **LONG QUESTION**

Given that the frequency dependent relative permittivity of a material is expressed as  $\varepsilon^*(\omega) = \varepsilon'(\omega) - i\varepsilon''(\omega)$  write down an expression for the loss tangent (tan  $\delta$ ) and briefly explain its significance. [3 marks]

For a particular material, up to angular frequencies  $\omega \gg \omega_0$ , it is found that

$$\varepsilon^*(\omega) = A + \frac{B}{(\omega_0 - \omega) + i\gamma\omega}$$
,

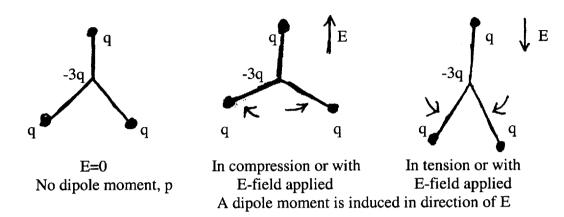
where A, B,  $\omega_0$  and  $\gamma$  are positive constants. Sketch the form of the real and imaginary components of  $\varepsilon^*(\omega)$  as a function of  $\omega$  indicating any key values. [9 marks]

If  $\omega_0 = 2 \times 10^{12} \,\mathrm{s}^{-1}$  and  $\gamma = 1$  at what frequency is there a maximum in  $\varepsilon''(\omega)$ ? [8 marks]

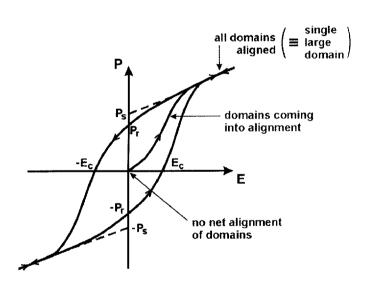
## **ANSWERS**

## **SHORT QUESTIONS**

a) The key requirement is that the structure must be **non-centrosymmetric**, i.e. not having inversion symmetry. There is no need for a permanent dipole moment. A system built from non-polar "building blocks" such as the molecule below would show the effect.



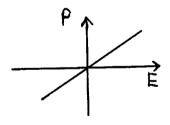
## b) Ferroelectric hysteresis diagram



 $P_S$  - spontaneous polarisation defined  $P_T$  - remanent polarisation  $P_S$  - coercive field  $P_S$  +ve

The figure on the left shows the situation with T below the Curie temperature. Above the Curie temperature the material reverts to paraelectric form with

$$P = \varepsilon_0 \chi E$$



#### LONG QUESTION

The definition of the loss tangent is  $\tan \delta = \frac{\varepsilon''}{\varepsilon'}$ . This is a measure of the energy dissipation (losses) within the material. If  $\varepsilon'' = 0$  there will clearly be no losses.

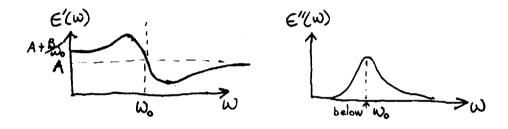
$$\varepsilon^{*}(\omega) = A + \frac{B}{(\omega_{0} - \omega) + i\gamma\omega} = A + \frac{B}{(\omega_{0} - \omega) + i\gamma\omega} \times \frac{(\omega_{0} - \omega) - i\gamma\omega}{(\omega_{0} - \omega) - i\gamma\omega}$$
$$= A + \frac{B(\omega_{0} - \omega)}{(\omega_{0} - \omega)^{2} + \gamma^{2}\omega^{2}} - i \cdot \frac{B\omega\gamma}{(\omega_{0} - \omega)^{2} + \gamma^{2}\omega^{2}}$$

Thus we have that the real part of  $\varepsilon^*(\omega) = \varepsilon'(\omega) = A + \frac{B(\omega_0 - \omega)}{(\omega_0 - \omega)^2 + \gamma^2 \omega^2}$  and the imaginary

component is

$$\varepsilon''(\omega) = \frac{B\gamma\omega}{(\omega_0 - \omega)^2 + \gamma^2\omega^2}.$$

 $\varepsilon'(\omega) = A + \frac{B}{\omega_0}$  when  $\omega = 0$ , drops to A when  $\omega = \omega_0$  and rises up to A again with  $\omega \gg \omega_0$ .  $\varepsilon''(\omega) \to 0$  at low and high frequencies and has a peak (see later) in between, below  $\omega_0$ .



$$\varepsilon''(\omega)$$
 peaks when  $\frac{d\varepsilon''}{d\omega} = 0 = \frac{B\gamma}{(\omega_0 - \omega)^2 + \gamma^2 \omega^2} - \frac{B\gamma\omega[-2(\omega_0 - \omega) + 2\gamma^2\omega]}{[(\omega_0 - \omega)^2 + \gamma^2\omega^2]^2}$ 

$$\Rightarrow 1 = \frac{\omega \left[ 2\gamma^2 \omega - 2(\omega_0 - \omega) \right]}{(\omega_0 - \omega)^2 + \gamma^2 \omega^2}$$
$$\Rightarrow \omega_0^2 + \omega^2 - 2\omega_0 \omega + \gamma^2 \omega^2 = 2\gamma^2 \omega^2 - 2\omega \omega_0 + 2\omega^2$$

$$\therefore \omega^2 (1 + \gamma^2) = \omega_0^2$$

Thus,  $\omega = \omega_0 / \sqrt{2} = 1.414 \times 10^{12} \,\text{s}^{-1}$  at the maximum with  $\gamma = 1$ .